Analysis of Capillary Water Migration Law of Compacted Loess in Ningxia

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Abstract
Capillary water is the main cause of freezing damage and collapsible damage of compacted loess. Therefore, researching capillary water migration law of compacted loess is the key to solve various damage in the infrastructure construction of loess. Different regions have different climatic conditions, which make the physical and mechanical properties of the loess is different. In order to reveal the capillary water migration law of compacted loess in Ningxia, the moisture migration law of compacted loess with different degrees of compaction was studied by using standpipe method. The results show that the migration rate of capillary water is rapid at the early stage and gradually became slower with the increase of time, which is negatively related to the degree of compaction and migration height. The maximum migration height of capillary water increases exponentially with the increase of compactness. Migration rate and migration height of capillary water are related to capillary water potential, gravitational potential, and pipe-resistance of capillary. In this study, the relational equation can predict capillary water distribution and the migration height of compacted loess was newly established. This equation can also provide a reference to reduce various damage and freeze-thaw effect in compacted loess.

Keywords: capillary water, compacted loess, compactness, saturation, relational equation

Introduction
Loess is special quaternary sediment, which has characteristics of porosity, collapsibility, and high permeability [1-4]. The loess distribution in China is located between 34° and 45° north latitude which is estimated about 4.9% of the world’s total distribution area of loess and loess-shape rocks, with a total area of approximately 630,000 square kilometers [5-7]. Therefore, the foundation engineering construction related to loess is inevitable, and a series of problems caused by the physical and mechanical characteristics of loess need to be solved, such as foundation settlement, collapse deformation, landslide, soil erosion, and freezing damage, which spreads throughout the loess distribution region [8-10]. Ningxia Hui Autonomous Region of China is located in the northern Loess Plateau, which belongs to serious collapsible loess

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regions [11-14]. It is cold and dry in winter, large areas of farmland are irrigated before winter, which makes the frost-heave of soil large and the rate of frost-heave reaches 13.0%, canals and subgrade projects are severely damaged by frost [15-17]. However, capillary moisture is the main source of water supply during the soil frost-heave process, which is an important factor affecting soil frost-heave deformation [18]. In order to reduce the freezing damage, satisfy the needs of production construction and theoretical research of compacted loess, investigating the capillary moisture migration law of compacted loess is necessary.

Previous studies have shown that the migration law of capillary water is related to temperature potential, gravitational potential, and matrix potential [19]. The temperature potential refers to the effect of temperature changes caused by the external environment on the migration direction, migration height and rate of capillary water. Gravity potential means that the self-gravity of capillary water has different effects on the migration law of capillary water in different directions. Matrix potential is related to the influence of different ionic and molecular attractive force on capillary water migration in different soils, which is caused by their different mineral components and physical and mechanical properties. Freeze-thaw cycles (FT) and dry-wet (TW) cycles are the main causes of damage to compacted loess. The freeze-thaw cycle is the main research direction of temperature potential on the migration law of capillary water, which is a seasonal process and exists widely in seasonal frozen ground regions. Meanwhile, the freeze-thaw cycle is usually accompanied by dry-wet cycle, both of which can decrease the mechanical properties of soils [20-24]. Capillary water migration rate in the compacted loess is inversely related to the number of dry-wet cycles, initial water content and compaction degree [25]. It is dry and windy in winter that capillary water migrates to ground surface due to strong evaporation. At the same time, the salt in the soil is also transported to the surface and accumulated under the action of capillary water [26]. When the temperature is lower than 0°C, the capillary water in the soil will gradually be transformed into solid ice from top to bottom of the ground, which will attract moisture of soil migrate to the frozen zone too [27, 28], the soil frosts heave and the volume will increase. As temperature increases, the water molecules between the soil particles are transformed from solid ice to liquid water. Meanwhile, the moisture content of soil increases, porosity increases. Accordingly, shear strength, compression strength, cementation between soil particles, compaction, and elastic modulus of the soil would be decreased during this process, all of which would cause collapsible deformation and uneven settlement of the soil [29].

The migration law of capillary water is also affected by gravitational potential. The migration rate of capillary water is negatively correlated with the migration height [30, 31]. The higher the migration, the greater the gravitational potential energy of the water molecules which can decrease the migration rate of moisture. The distribution of capillary water is also related to the nature of the soil. Different mineral components and ionic content will cause differences in soil matrix suction. Capillary water migration equation and simplified equation based on particle size distribution can effectively describe the soil water retention curve and determine the soil hydraulic conductivity [32]. The study of geotechnical characteristics of loess shows that open pores in the soil are the main reason for loess collapsing [33]. Higher compaction degree and smaller water content can effectively reduce the rate of water migration and avoid the collapse of the loess [34].

Generally speaking, different soils have various physical and chemical properties [35, 36], such as compaction, saturation, moisture content, dry density, thickness of combined water film, and so on. Different matrix potential can influence migration height and rate of capillary water too. In recent years, more and more scholars pay emphasis on the improvement of loess collapsible by adding additives loess and better drainage system, which can effectively improve the collapsible damage of the compacted loess [37-40].

Soil quality is an important factor in controlling capillary water migration. However, the interaction between the external environment and the soil will affect the soil quality. Accordingly, the hydro-geographic conditions in different regions will have different effects on the physical and mechanical properties of the soil, the physical and mechanical characteristics of loess in different regions are different. Ningxia loess has smaller content of hydrophilic minerals and smaller amount of clay, so it has a different capillary water migration law from other regions. However, the research on the capillary water migration law of Ningxia compacted loess is still in its infancy. In order to understand the capillary water migration law of Ningxia compacted loess and determine the soil hydraulic conductivity [32]. The study of geotechnical characteristics of loess are shown

Materials and Methods

Experimental Materials

According to the Specification of Soil Test (SL237-1999), the loess used in the test was taken from Tongxin County of Ningxia Hui Autonomous Region, the physical and mechanical indexes of the loess are shown
in Table 1. XRD analysis showed that the main minerals were quartz, calcite, Na₃Al₅Si₅O₁₄, and mica, as shown in Fig. 1. The particle size distribution is shown in Fig. 2. It is mainly silt-grained soil of 0.005 mm ~0.075 mm, accounting for 81.3%, and the clay-grained content is small, about 13.9%. The SEM micro-morphology of the loess particles is shown in Fig. 3. The morphology of loess particles is mainly granular, angular, elliptical, and surface is slightly convex. The surface of the coarse powder particles is adhered by small sticky particles or colloidal particles. There are few cohesive particles with a particle size smaller than 5 um.

Experimental Methods

Experimental Scheme

The physical and mechanical indexes of samples are shown in Table 2. the compaction degree was set at four levels of 0.86, 0.90, 0.94, and 0.98. At temperature of 20±1ºC, studied the capillary moisture migration height of loess with different compaction degrees. The capillary moisture migration rate is fast in the early period and slower in the later period, so the observation interval is set relatively short in the early days and long when it is stable or near the top of the tube. the early data observation interval was 1d, 3d, 7d, 12d respectively. when capillary action is stable or near the top of the tube, further data are observed at every 12d until 72d. In order to facilitate the preparation of samples and observe the position of the vertex about capillary moisture, the water content used in the sample preparation was \( w_0 = 8.0\% \).

Preparation of Samples

The loess was air-dried and crushed, and water was added according to the moisture content set in the plan. It was then mixed evenly and put in a sealed bag, and placed in a moisturizing container for not less than 24 hours to fully mixed the soil particles and water. According to the designed compaction and the thickness of each layer (5 cm), the quality of wet soil in each layer was calculated, and compacted each layer in an organic-glass sample tube. The sample is 10 cm in diameter and 200 cm in height.

Capillary Water Migration Test

The migration height of capillary moisture was measured by the standpipe method. The test device is shown in Fig. 4. The inner diameter of the standpipe
was 10 cm and the height was 200 cm. A ruler was attached upward from 10 cm at the bottom of the standpipe to locate the position of the vertex of capillary moisture. A 10 mm hole was drilled every 10 cm from 15 cm up from the bottom to determine the moisture content of the soil. The top of the standpipe was wrapped with a plastic film with small holes to prevent the water in the soil sample at the top of the pipe from evaporating too quickly. A 400-mesh gauze pad was placed on the bottom to prevent soil from escaping into the water. The bottom of the water storage tank was covered with fine-stones of 5 cm, and an overflow hole was opened at 15 cm. The thin stream continuously replenishes water, and the depth of the vertical pipe in the water was always maintained at 10 cm. The migration height of capillary water was observed by the direct-observation method under the guidance of technical code (SL237-1999), according to the color change of the soil sample and the ruler attached to the vertical pipe.

The moisture content sensor can continuously monitor the dynamic changes of soil moisture, but there are many factors that affect the accuracy of the measurement, and there are certain measurement errors [41-45]. Especially for saline soils, the measurement results are significantly diverse due to different salt content. Although the quality-method cannot continuously monitor the soil moisture content, it has few influencing factors and high measurement accuracy.

The content of soluble salt in loess is more than others, and it is unevenly distributed due to migration of capillary moisture [46-48]. In the study of soil freeze-thaw effect, the most concerned is the steady-state moisture content when capillary moisture migrations to reach stability, so the quality-method was used to determine the moisture content. After the capillary moisture migration height was stable, samples were taken at about 2 cm and 5 cm from the tube wall, and the average value was used as the measurement result.

### Results and Discussion

#### Analysis of Water Migration

The relationship between the capillary moisture migration height $h$ and time $t$ of loess samples with different compaction degrees is shown in Fig. 5, and the moisture migration rate $v$ of the corresponding period is shown in Fig. 6.

It can be seen from Fig. 5 and Fig. 6 that the early migration of capillary moisture in the compacted loess was fast, especially on the first day, the sample with a compaction degree of 0.86 had a capillary moisture migration rate of 60 cm/day. With the increase of time, the migration rate of capillary moisture decreased rapidly. The migration rate at the 2~3d was only 1/2.5~1/4.7 of the migration rate at the 1d, which had dropped by 60%~78%. After 36d, the rate of capillary moisture migration was less than 1.0 cm/day. The

<table>
<thead>
<tr>
<th>Sample number</th>
<th>Degree of compaction $\lambda$</th>
<th>Dry density $\rho_d$(g/cm$^3$)</th>
<th>Porosity ratio $e$</th>
<th>Water content $w_o$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.86</td>
<td>1.48</td>
<td>0.84</td>
<td>8.0</td>
</tr>
<tr>
<td>2</td>
<td>0.90</td>
<td>1.55</td>
<td>0.76</td>
<td>8.0</td>
</tr>
<tr>
<td>3</td>
<td>0.94</td>
<td>1.62</td>
<td>0.68</td>
<td>8.0</td>
</tr>
<tr>
<td>4</td>
<td>0.98</td>
<td>1.69</td>
<td>0.61</td>
<td>8.0</td>
</tr>
</tbody>
</table>

Fig. 4. The device of capillary water migration test.

Fig. 5. Relationship between capillary moisture migration height and time.
In the early stage of capillary moisture migration, the resistance of the pipe wall increased, and the capillary moisture migration rate decreased rapidly. Higher compactness of loess results in a reduction of the capillary while increasing the capillary moisture potential and the pipe wall resistance. when compaction degree is greater than 0.86, the capillary wall resistance of the loess increases faster than the capillary moisture potential with the increase of the compaction degree, the capillary moisture migration rate decreases, and the time to reach the maximum height was increased.

Fig. 5 shows that the capillary moisture migration height $h$ and time $t$ of each sample show a clear hyperbolic relationship.

$$h = \frac{t}{a + h_u}$$

(1)

In the Equation 1: $a$ and $h_u$ are the fitting coefficients to be determined, $h_u$ is the extreme value of $h$ when $t$ tends to infinity, that is, the maximum height of capillary moisture, cm.

The fitting coefficients $a$ and $h_u$ and the correlation coefficient $R^2$ of the capillary moisture migration equation of each sample are shown in Table 3, $R^2$ in Table 3 are all close to 1.0, and the relationship between capillary moisture migration height and time is fitted with a hyperbolic relationship, which has a high correlation of fit.

Using the least squares method to further fit the relationship among $a$, $h_u$, compaction degree $\lambda_c$ and porosity $e$ (Fig. 7), which can get:

$$h_u = 216.33\lambda_c^{0.7099} = 184.55e^{-0.2984}$$

(2)

$$a = 15.0\lambda_c^{10.212} = 1.532e^{-4.2791}$$

(3)

The correlation coefficient $R^2$ of fitting coefficient $a$ and $h_u$ has an obvious correlation with compaction degree $\lambda_c$ and porosity $e$, which are all close to 1. From Equation 2 and Equation 3, it can be seen that the maximum migration height of capillary moisture increases exponentially with the degree of compaction, decreases with the exponential decreasing power ratio of porosity, and It is consistent with the Hazen formula $h_i = Ce^{3}$ for estimating the maximum migration height of sandy capillary moisture [52]. When the radius of the pores between the particles is less than 2.75 μm, the capillary moisture phenomenon does not occur, and the corresponding particle size is 0.0024 mm [53]. The grain composition of Ningxia loess is mainly powder and less than 4% of particles smaller than 0.002 mm. The mineral composition is mainly quartz, calcite and mica with small hydrophilicity, the combined water film is thin, even in the most compact state, there are few pores with a radius less than 2.75 μm, and the path of capillary moisture migration will not be blocked.
migration in capillary moisture increases with the degree of compaction. The maximum migration height of capillary moisture in compacted loess depends mainly on the potential energy of capillary moisture and has nothing to do with capillary wall resistance.

\[ h_u = 184.55e^{-0.2984} \]

In the equation \( h_u = 184.55e^{-0.2984} \), the absolute value of the index of the void ratio \( e \) is 0.2984, which is far smaller than the absolute value of the index of \( e = 1.0 \) in the Hazen formula. It is difficult to choose a suitable value of \( c \), and the Hazen equation is used to accurately predict the capillary moisture migration height.

Table 3. The fitting parameter capillary migration model.

<table>
<thead>
<tr>
<th>Sample number</th>
<th>Fitting coefficient ( a )</th>
<th>Maximum height of capillary moisture ( h_u ) (cm)</th>
<th>Correlation coefficient ( R^2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3.332</td>
<td>195.8</td>
<td>0.99</td>
</tr>
<tr>
<td>2</td>
<td>5.060</td>
<td>199.2</td>
<td>0.99</td>
</tr>
<tr>
<td>3</td>
<td>7.259</td>
<td>205.5</td>
<td>0.99</td>
</tr>
<tr>
<td>4</td>
<td>13.041</td>
<td>214.9</td>
<td>0.99</td>
</tr>
</tbody>
</table>

Fig. 7. Fitting analysis of regression parameters.

Table 4. Prediction and verification of capillary moisture migration height.

<table>
<thead>
<tr>
<th>Samples number</th>
<th>Measured value (cm)</th>
<th>Predicted value (cm)</th>
<th>Residuals (cm)</th>
<th>Relative residuals (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>178.4</td>
<td>175.0</td>
<td>3.4</td>
<td>1.9</td>
</tr>
<tr>
<td>2</td>
<td>169.8</td>
<td>168.7</td>
<td>1.1</td>
<td>0.6</td>
</tr>
<tr>
<td>3</td>
<td>161.6</td>
<td>163.2</td>
<td>-1.6</td>
<td>-1.0</td>
</tr>
<tr>
<td>4</td>
<td>146.4</td>
<td>146.6</td>
<td>-0.2</td>
<td>-0.1</td>
</tr>
</tbody>
</table>
predict the maximum height of capillary moisture in Ningxia loess. The maximum migration of capillary moisture in compacted loess is affected by porosity, but it is far less sensitive than in sand.

In order to verify the reliability of the equation, the capillary moisture migration height of each group of samples was measured during the test. The measured values of the capillary moisture migration height of each group of samples for 28d, the equation predicted values, and the residuals and relative residuals of the measured and predicted values are listed in Table 5. It can be seen from Table 4 that the relative residuals between the predicted value and the measured value of the capillary moisture migration height equation are within 5%, and the equation prediction results are accurate and reliable.

Analysis of Capillary Moisture Distribution

Fig. 8 shows the steady-state moisture content distribution of the loess samples with different degrees of compaction, and Fig. 8 is the saturation distribution. It is observed from Fig. 8 and Fig. 9 that the moisture content of each test point of the sample is significantly larger than the initial moisture content of the sample, this phenomenon indicated that moisture of the four samples had migration to the top of the standpipe. The water content and saturation decreased with the increase of height. Within the range of 65 cm from the water level, the water content and saturation changed slowly along with migration height, and the saturation can reach more than 80%, the other part above 65 cm decreased slightly with the increase of height. The moisture content of the sample at the same height decreased obviously with the increase of the compaction degree. The saturation increased with the increase of the compaction degree, but the change of saturation was not obvious with the increase of compaction in the regions with high saturation.

From Table 5, Table 6, Table 7 and Table 8, regression analysis and optimization were applied to obtain the distribution equations of moisture content and saturation along with the height of loess with different compaction degrees.

\[
\begin{align*}
\text{w} &= 63.8 - 0.0370h - 43.3472 \lambda_c \\
S_r &= 89.9 - 0.1370h
\end{align*}
\] (4) (5)

Table 5. Variance analysis results of water content.

<table>
<thead>
<tr>
<th></th>
<th>Degree of freedom</th>
<th>Error sum of squares</th>
<th>Mean square deviation</th>
<th>F</th>
<th>Significance F</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regression analysis</td>
<td>1</td>
<td>909.883</td>
<td>909.883</td>
<td>1031.009</td>
<td>5.8807E-16</td>
</tr>
<tr>
<td>Residual error</td>
<td>16</td>
<td>14.1203</td>
<td>0.8825</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>17</td>
<td>924.0033</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Note: because the correlation between saturation and compaction is very low, the average value of the four samples is taken as the result for regression analysis, the degree of freedom is 17.

Table 6. Regression parameters of water content.

<table>
<thead>
<tr>
<th>Coefficients</th>
<th>Standard error</th>
<th>t Stat</th>
<th>P-value</th>
<th>Lower 95%</th>
<th>Upper 95%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>89.9326</td>
<td>0.4434</td>
<td>202.8422</td>
<td>88.9927</td>
<td>90.8725</td>
</tr>
<tr>
<td>Height</td>
<td>-0.1370</td>
<td>0.0043</td>
<td>-32.1093</td>
<td>-0.1461</td>
<td>-0.1280</td>
</tr>
</tbody>
</table>
The significance parameter $F$ of the water content relationship equation is 841.911, the correlation coefficient $R^2$ is 0.96, and the critical value $F_{0.99} = 4.79$. The $F$ of the saturation relationship equation is 1031.0, the correlation coefficient is 0.98, and the critical value is $F_{0.99} = 8.53$. It can be concluded from the above numerical analysis. Both of the water content relationship equation and the saturation relationship equation were highly significant and have a good correlation with factors. The saturation distribution equation has nothing to do with compaction, which indicated that the effect of compaction on saturation is not obvious.

The steady-state water content distribution curve of soil in the capillary moisture migration area is also the soil-water characteristic curve [54, 55]. Equation 4 and Equation 5 are soil-water characteristic curves characterized respectively by mass water content and saturation. The soil-water characteristic curve characterized by saturation which had nothing to do with compaction. “In a wide range of matric suction, saturation is not affected by porosity” [56-58], which can be mutually proved by Equation 5.

In order to compare and analyze the degree of influence of compaction on water content and saturation, analysis of variance was performed respectively on water content and saturation. The distribution of significance parameter $F$ along the height is shown in Fig. 10.

Fig. 10 revealed that the $F$ of the saturation was much smaller than the $F$ of the water content in the range of moisture migration height, which indicated that the impact of the compaction on the saturation was less obvious than the effect of the water content. The $F$ about water content was all greater than $F_{0.90}$, and gradually increased from top to bottom. The effect of compaction on water content had increased rapidly from obvious to very obvious and then reach to the most obvious. The part of obvious and very obvious account for a large proportion, was about 85%. The $F$ about saturation were all less than $F_{0.90}$, and the impact of compaction on saturation was not obvious, mainly because saturation was a combination of water content and porosity. According to the variance theory, if the influence of a factor was not obvious, it can be seen that the factor has no effect. Therefore, when the degree of compaction of the loess is greater than 0.86, the effect of the compaction degree on the soil saturation in the capillary moisture migration area can be ignored.

It can be inferred that loess has a limited increase or decrease in density after the compaction due to changes in load, temperature, humidity, and other factors, the steady-state water content in the capillary moisture migration zone increases and decreases, while the saturation remains unchanged. This inference provides a theoretical basis for the study of the effects of freeze-thaw cycles of unsaturated compacted loess on the hydration cycle.

### Conclusions

This paper presents a study under the condition that the compaction degree is not less than 0.86, with a powder content of about 80.0% and the main mineral composition is mainly composed of Quartz, Calcite, Na$_2$Al$_5$Si$_3$O$_{16}$ and Mica. The migration of capillary

### Table 7. Variance analysis results of saturation.

<table>
<thead>
<tr>
<th></th>
<th>Degree of freedom</th>
<th>Error sum of squares</th>
<th>Mean square deviation</th>
<th>F</th>
<th>Significance F</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regression analysis</td>
<td>2</td>
<td>536.3223</td>
<td>268.161</td>
<td>841.911</td>
<td>3.399E-49</td>
</tr>
<tr>
<td>Residual error</td>
<td>69</td>
<td>21.9775</td>
<td>0.3185</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>71</td>
<td>558.2999</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### Table 8. Regression parameters of saturation.

<table>
<thead>
<tr>
<th></th>
<th>Coefficients</th>
<th>Standard error</th>
<th>t Stat</th>
<th>P-value</th>
<th>Lower 95%</th>
<th>Upper 95%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>63.786</td>
<td>1.375</td>
<td>46.399</td>
<td>9.254E-54</td>
<td>61.043</td>
<td>66.528</td>
</tr>
<tr>
<td>Height</td>
<td>-0.037</td>
<td>0.001</td>
<td>-28.885</td>
<td>2.892E-40</td>
<td>-0.039</td>
<td>-0.034</td>
</tr>
<tr>
<td>Degree of compaction $\lambda_c$</td>
<td>-43.347</td>
<td>1.487</td>
<td>-29.146</td>
<td>1.628E-40</td>
<td>-46.314</td>
<td>-40.380</td>
</tr>
</tbody>
</table>
moisture in Ningxia compacted loess is studied by using the standpipe method, and the following conclusions are drawn:

(1) The capillary moisture migration height of Ningxia compacted loess is larger than 200cm. The maximum migration height increases exponentially with the increase of compactness.

(2) The effect of compactness on saturation is not obvious. Accordingly, it can be assumed that the saturation of the loess is almost unchanged after freeze-thaw cycles, when studying the effects of freeze-thaw cycles on capillary water migration laws of loess.

(3) The moisture content decreases with the increase of height, and the moisture content decrease rate increases with the increase of height. The moisture content of the sample at the same height decreases as the degree of compaction increases.

(4) The newly established equations can effectively reflect the relationship between saturation, compaction and capillary moisture migration height, and provide a theoretical basis for the study of freeze-thaw deformation of loess engineering.

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Conflict of Interest

The authors declare no conflict of interest.

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