

and the imperfection of government regulation [3, 4]. Against this background, how to reduce environmental pollutant emissions has become a fundamentally important research topic in the field of environmental safety management.

To realize green development, the enterprises that produce harmful substances that pollute the environment during production are required to install pollution control equipment. This equipment usually is costly. Because of limited resources, the enterprise may not install the pollution control equipment voluntarily. Consequently, the government has to take supervisory measures to inspect the enterprise's green production. If a government has discovered the illegal behavior of an enterprise, it is responsible for cleanup and penalty costs. In China, the local government usually is responsible for green production supervision because the enterprise's income contributes to the performance of these local governments. Also, local government's supervision measures affect the enterprise's income, which demonstrates that a strategic interaction in fact exists between the government and the enterprise.

The traditional game model has been used to analyze this strategic interaction between the government and the enterprise in the evaluation of supervision problems. The government and the enterprise can reach an equilibrium by balancing costs and benefits [5]. A multistage game model also has been proposed to analyze the strategic interaction among the government, the manufacture, and the energy supplier in a residential energy-efficiency program. The impact of rebound, consumer behavior, and government policies (tax policies and subsidy) have been considered using the game model [6]. Similarly, Ma et al. has studied how subsidy affects the game between the enterprise and the government [7]. The impact of some other factors, such as a cooperative contract between the manufacture and the retailer [7, 8], and the social welfare of an enterprise's green production decision, also have been analyzed [9].

Because of the bounded rationality of the players and the dynamic characteristics of the game [10], the evolutionary game has been proposed and used to analyze strategic interactions between the government and the enterprise in government supervision problems. Extensive researches have investigated China's coal mine safety inspection system by using an evolutionary game [11, 12, 13]. Specific to green production supervision problems, the impact of various carbon taxes and subsidies on the enterprise's low-carbon production methods was analyzed by using the evolutionary game model [14, 15]. Jiang et al. considered the multiagent environmental regulation problem under Chinese fiscal decentralization [16]. In their study, they used evolutionary game theory to unpack the interactive strategies of the polluting enterprise, local government regulators, and central government planners. Cui et al. studied the green agriculture game through building

an evolutionary game between the government and the farmer [17].

These researches have shown that the impact of many external influencing factors on the game between the government and the polluting enterprise have been studied extensively. The external influencing factors include government subsidies, tax policies, consumer behavior, public participation. In addition to these external factors, the enterprise imposes many internal factors as well. The enterprise's goal is profit maximization. As pollution control equipment demands a large amount of resources and the total resources of the enterprise are limited, the impact of the equipment cost on production yield becomes an important factor.

Against this background, in this paper, we studied the green production supervision problem with consideration for the limited resources of the enterprise. In light of the bounded rationality of the players, we used evolutionary game theory to build the supervision game model.

This paper is organized as follows. Section 2 provides the problem description, assumptions, and notations of this paper. Section 3 builds the evolutionary game model of the green production supervision problem. Section 4 provides the analysis of the evolutionary stable strategies of the game. Section 5 gives the impact analysis of some of the parameters for the evolutionary stable strategies of the game. Last, conclusions are presented in Section 6.

Model

Problem Description, Assumptions and Notations

The players in a green production supervision game include the manufacturing enterprise and the government regulator. Normally, the government requires the enterprise to install pollution control equipment. The cost of this equipment is called the green production input cost of the enterprise. This required pollution control equipment may not be installed by the enterprise, however, because of limited resources and the opportunity benefit realized by not installing the equipment. Under this circumstance, the government takes supervisory measures to ensure compliance of the enterprise's green production.

In the game between the government and the enterprise, the enterprise chooses whether to implement green production. Therefore, the strategy space of the enterprise is defined as $T_c = \{Green, Not\ Green\}$. Assume the total resources of the enterprise are R , which can generate profit I . The green production input cost is S_c , which can generate profit S_c^h if it is put into production; h denotes the output coefficient and $h > 0$. If the enterprise implements green production, then its production profit is $I - S_c^h$. And if the enterprise does not implement green production, its production profit is I because all the resources are invested into production.

Results and Discussion

Evolutionary Stable Strategy of the Green Production Supervision Game

Solving $\begin{cases} \frac{dx}{dt} = 0 \\ \frac{dy}{dt} = 0 \end{cases}$, we obtained five local equilibriums

of the two-population replicator dynamics model, which were as follows: (0,0), (0,1), (1,0), (1,1), and (x^*, y^*) .

$$x^* = \frac{(1-P)E + PL_c + Pr_g + r_g - S_c^h - S_g}{(1-P)E + PL_c + Pr_g + r_g - S_c^h},$$

$$y^* = \frac{(1-\tau)S_c^h - P(L_c + F_c)}{(1-\tau)S_c^h + 2r_c - P(L_c + F_c)}$$

These five local equilibriums may not be the evolutionarily stable strategy (ESS) of the replicator dynamics system. According to the method proposed by Friedman (1998), analyzing the Jacobian matrix of the differential equation can allow you to judge whether a local equilibrium is an ESS. The Jacobian matrix of a differential equation J is as follows:

$$J = \begin{bmatrix} \frac{\partial g(x)}{\partial x} & \frac{\partial g(x)}{\partial y} \\ \frac{\partial g(y)}{\partial x} & \frac{\partial g(y)}{\partial y} \end{bmatrix} = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix} \quad (5)$$

If the local equilibrium satisfies the following two conditions, then it is the ESS of the system.

Condition (1): $\det J = \begin{vmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{vmatrix} = a_{11}a_{22} - a_{12}a_{21} > 0$,

and

Condition (2): $tr J = a_{11} + a_{22} < 0$.

Table 2. The values of a_{11} , a_{12} , a_{21} , and a_{22} in each local equilibrium.

Local equilibrium	a_{11}	a_{12}	a_{21}	a_{22}
(0,0)	$-(1-\tau)S_c^h + P(L_c - F_c)$	0	0	$-S_c^h - S_g + (1-P)E + PL_c + (1+P)r_g$
(0,1)	$2r_c$	0	0	$S_c^h + S_g - (1-P)E - PL_c - (1+P)r_g$
(1,0)	$(1-\tau)S_c^h - P(L_c + F_c)$	0	0	$-S_g$
(1,1)	$-2r_c$	0	0	S_g
(x^*, y^*)	0	A	B	0

where:

$$a_{11} = (1-2x)\{y[(1-\tau)S_c^h + 2r_c - P(L_c + F_c)] + P(L_c + F_c) - (1-\tau)S_c^h\}$$

$$a_{12} = x(1-x)[(1-\tau)S_c^h + 2r_c - P(L_c + F_c)]$$

$$a_{21} = y(1-y)[S_c^h - (1-P)E - PL_c - Pr_g - r_g]$$

$$a_{22} = (1-2y)\{x[S_c^h - (1-P)E - PL_c - Pr_g - r_g] - [S_c^h - (1-P)E + S_g - PL_c - Pr_g - r_g]\}$$

In the problem of green production supervision game, the values of a_{11} , a_{12} , a_{21} , and a_{22} in each local equilibrium are given in Table 2.

In Table 2,

$$A = x^*(1-x^*)[(1-\tau)S_c^h + 2r_c - PL_c - PF_c]$$

$$B = y^*(1-y^*)[S_c^h - (1-P)E - PL_c - Pr_g - r_g]$$

In this paper, we assumed environmental pollution occurred only when an enterprise's decision was not green, and the government's decision was weak supervision. Under the other conditions, the enterprises all installed pollution control equipment voluntarily or were forced. Before analyzing the ESS of the system, we proposed the following definition of "failed supervision."

Definition 1: The condition that the enterprise's decision is not green, and the government's decision is weak supervision is defined as failed supervision.

According to the definition of failed supervision, it was evident that the probability of failed supervision was $P_F = (1-x)(1-y)$. Once the system obtained the ESS, the probability of failed supervision also tended to stabilize.

According to Table 2, the ESS of the green production supervision game model proposed in this paper is shown in Proposition 1.

Proposition 1:

case (a): If $F_c < \frac{(1-\tau)S_c^h}{P} - L_c$ and $S_g > (1-P)E + PL_c + (1+P)r_g - S_c^h$, the ESS of the system is (0,0).

case (b): If $F_c < \frac{(1-\tau)S_c^h}{P} - L_c$ and $S_g < (1-P)E$
 $+ PL_c + (1+P)r_g - S_c^h$, the system is in periodical
 fluctuations.

case (c): If $F_c > \frac{(1-\tau)S_c^h}{P} - L_c$ and $S_g < (1-P)E$
 $+ PL_c + (1+P)r_g - S_c^h$, the ESS of the system is (1,0).

case (d): If $F_c > \frac{(1-\tau)S_c^h}{P} - L_c$ and $S_g > (1-P)E$
 $+ PL_c + (1+P)r_g - S_c^h$, the ESS of the system is (1,0).

To better understand the trends of evolution, a simulation analysis is shown in Fig. 2. We set the baseline values of the parameters as $\tau = 0.2$, $h = 1$, $S_c = 5$, $P = 0.3$, $L_c = 7$, $E = 5$, $r_g = 2$, and $r_c = 2$. We set F_c , S_g according to the four cases provided in Proposition 1.

Proposition 1 and Fig. 1 show the ESS of the green production supervision game. Under the condition of case (a), the ESS was (0,0). The ESS was (1,0) under the condition of case (c) and case (d). Under the condition of case (b), the replication dynamic system showed a fluctuating trend. This meant that the system had a stable limit cycle, but it was not asymptotically stable (Liu et al., 2015). From the point of the stable state of failed supervision probability, it was 1 under case (a) and 0 under case (c) and case (d). Under case (b), the probability of failed supervision fluctuated because the system fluctuated. We assumed that the environmental hazards happened only when they experienced failed supervision. Hence, reducing the probability of failed

supervision was key to reducing environmental hazards. Against this background, the ESS of case (c) and case (d) was better than that of case (b). The ESS of case (b) was better than that of case (a).

The probability of failed supervision was not 0 under the condition of case (a) and case (b), which meant that the environmental hazards may have happened under these conditions. To reduce environmental hazards, it was important to impel the system to transfer from case (a) and case (b) to case (c) or case (d). The impact of the analysis of some of the parameters on the ESS is explained in Section 5. On the basis of the impact analysis, we proposed corresponding supervision policy suggestions for the government with the goal of improving environmental quality.

Discussion: The Impact Analysis of Supervisory Parameters on the ESS

The Impact Analysis of Penalty F_c

According to Proposition 1, if $F_c > \frac{(1-\tau)S_c^h}{P} - L_c$,

then the ESS of the system would be (1,0) and the failed supervision probability would be 0. Otherwise, it would be possible for the environmental hazard to occur. From this point of view, increasing the penalty on the enterprise when environmental hazards are discovered

under certain conditions (which is $F_c > \frac{(1-\tau)S_c^h}{P} - L_c$) would reduce the failed supervision probability.

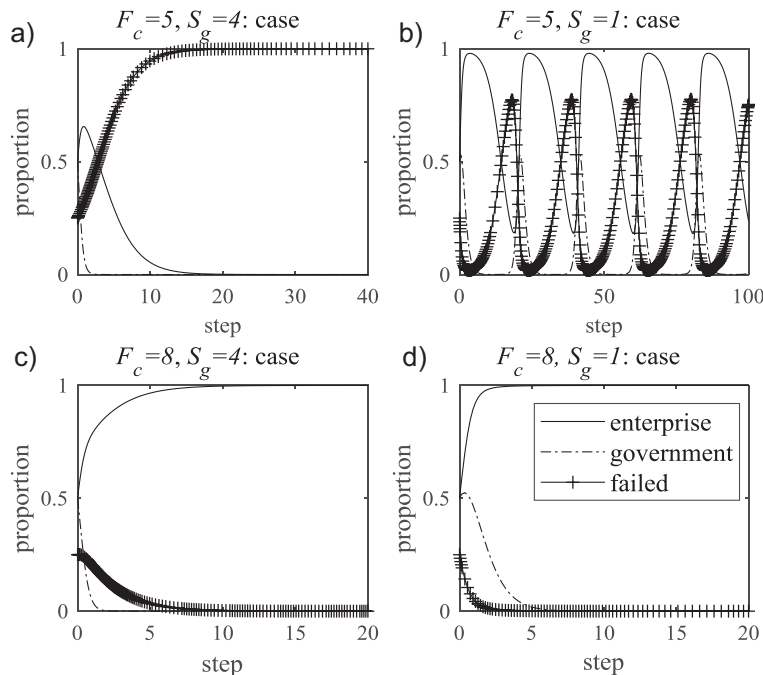


Fig. 2. The evolutionary trend of the green production supervision game.

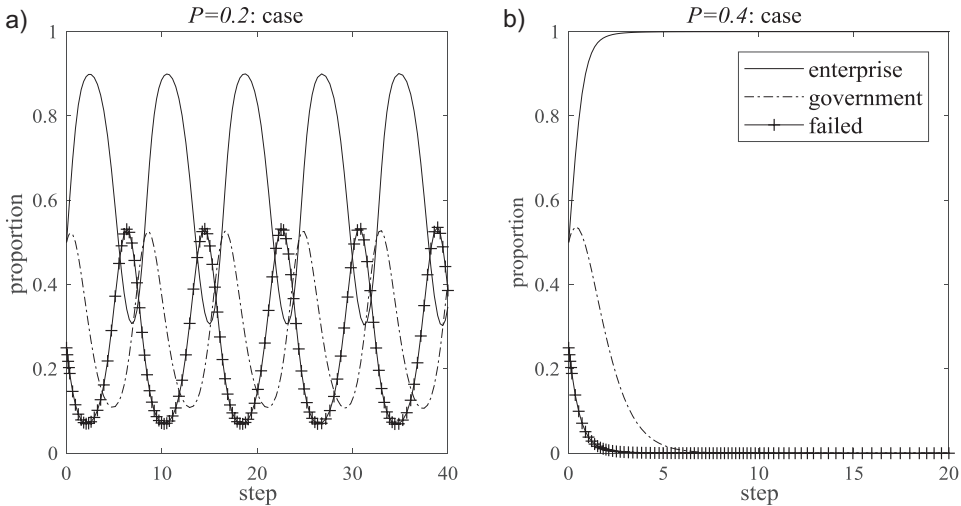


Fig. 6. The impact of P on the ESS ($\tau = 0.2, h = 1, S_c = 5, L_c = 7, E = 5, r_g = 2, r_c = 2, F_c = 5, S_g = 1$).

the media to supervision are good methods to improve the probability that pollution will be discovered by the public [18-20]. Against this background, the government can improve the probability that pollution was discovered through introducing the public and the media to supervision. Then, the environmental hazard would be reduced. The impact of probability P on the ESS of the green production supervision game is illustrated in Fig. 6. Only one figure is presented here, this is because the two change trends under the given conditions are the same.

Conclusions

Green production is an important development trend not only in China but also around the world. Installing pollution control equipment is one way to control the emission of pollutants and realize green production. Because of the costs associated with this pollution control equipment and the information asymmetry, the enterprise may not be willing or able to install the equipment voluntarily. Against this background, we studied the supervision game between the government’s supervision strategy and the enterprise’s green production strategy. Unlike previous studies, we considered the impact of the enterprise’s limited resources, which was an internal factor, on the supervision game. We built an evolutionary game model between the government and the enterprise and provided the ESS of the model. Because pollution tended to occur only when the government’s decision was weak supervision and the enterprise’s decision was not green, this paper analyzed the probability of this condition and defined this condition as failed supervision. Reducing the probability of failed supervision helped reduce environmental hazards. On the basis of the ESS under given conditions, we also analyzed the impact of some

parameters on the ESS. The impact analysis revealed several ways to improve the ESS and to reduce the probability of failed supervision: (1) increasing the penalty on the enterprise once pollution was discovered, (2) reducing the mandatory green production cost reasonably, and (3) increasing the taxation ratio and the probability that pollution would be discovered through introducing the public and the media into supervision. This paper outlined the specific conditions of changing these parameters with the goal of reducing failed supervision probability. In general, the results of this paper provide decision-making support for the government on green production supervision, which, in turn, will help to reduce environmental hazards.

Acknowledgement

This study was supported by the Social Science Foundation of Beijing (19GLC066); the National Natural Science Foundation of China (71801137); the Development of University Connotation Scientific Research Level Promotion Project at Beijing Information Science and Technology University (2019KYNH216).

Conflict of Interest

The authors declare no conflict of interest.

References

1. WANG R. The influence of environmental regulation on the efficiency of China’s regional green economy based on the GMM model. *Polish Journal of Environmental Studies*. **29** (3), 2395, **2020**.
2. BEAVIS B., WALKER M. Random wastes, imperfect monitoring and environmental quality standards[J]. *Journal of Public Economics*. **21** (3), 377, **1983**.

3. KIM S.H. Time to come clean? Disclosure and inspection policies for green production[J]. *Operations Research*. **63** (1), 1, **2015**.
4. WANG S., SUN P., de VERICOURT F. Inducing environmental disclosures: A dynamic mechanism design approach[J]. *Operations Research*. **64** (2), 371, **2016**.
5. SCHOL J.T. Cooperative regulatory enforcement and the politics of administrative effectiveness. *The American Political Science Review*. **85** (1), 115, **1991**.
6. SOROUGH S., MORTEZA R.B. A game theoretic approach for assessing residential energy-efficiency program considering rebound, consumer behavior, and government policies. *Applied Energy*. **233-234**, 44, **2019**.
7. MA W., ZHANG R., CHAI S. What drives green innovation? A game theoretic analysis of government subsidy and cooperation contract. *Sustainability*. **11**, 5584, **2019**.
8. JEONG E.B., PARK G.W., YOO S.H. Incentive mechanism for sustainable improvement in a supply chain. *Sustainability*. **11**, 3508, **2019**.
9. ZHANG Z., WANG Y., MENG Q., LUAN X. Impacts of green production decision on social welfare. *Sustainability*. **11**, 453, **2019**.
10. FRIEDMAN D. On economic applications of evolutionary game theory. *Journal of Evolutionary Economics*. **8** (1), 15, **1998**.
11. LIU D., XIAO X., LI H., WANG W. Historical evolution and benefit-cost explanation of periodical fluctuation in coal mine safety supervision: An evolutionary game analysis framework. *European Journal of Operational Research*. **243** (3), 974, **2015**.
12. LIU Q., LI X., HASSALL M. Evolutionary game analysis and stability control scenarios of coal mine safety inspection system in China based on system dynamics. *Safety Science*. **80**, 13, **2015**.
13. LIU Q., LI X., MENG X. Effectiveness research on the multi-player evolutionary game of coal-mine T safety regulation in China based on system dynamics. *Safety Science*. **111**, 224, **2019**.
14. CHEN W., HU Z.H. Using evolutionary game theory to study governments and manufacturers' behavioral strategies under various carbon taxes and subsidies. *Journal of Cleaner Production*. **201**, 123, **2018**.
15. FAN R., DONG L., YANG W., SUN J. Study on the optimal supervision strategy of government low-carbon subsidy and the corresponding efficiency and stability in the small-world network context. *Journal of Cleaner Production*. **168**, 536, **2017**.
16. JIANG K., YOU D., MERRILL R., Li Z. Implementation of a multi-agent environmental regulation strategy under Chinese fiscal decentralization: An evolutionary game theoretical approach. *Journal of Cleaner Production*. **214**, 902, **2019**.
17. CUI H., ZHAO T., TAO P. Evolutionary game study on the development of green agriculture in china based on ambidexterity theory perspective. *Polish Journal of Environmental Studies*. **28** (3), 1093, **2019**.
18. LI L., XIA X., CHEN B., SUN L. Public participation in achieving sustainable development goals in China: evidence from the practice of air pollution control. *Journal of cleaner production*. **201**, 499, **2018**.
19. TILT B. China' s air pollution crisis: science and policy perspectives. *Environmental science & policy*. **92**, 275, **2019**.
20. TANG Z., TANG J.T. Can the media discipline Chinese firms' pollution behaviors? The mediating effects of the public and government. *Journal of management*. **42**(6), 1700, **2016**.