Optimization of Turbidity and COD Removal from Pharmaceutical Wastewater by Electrocoagulation. Isotherm Modeling and Cost Analysis

Hadjira Kermet-Said*, Nadji Moulai-Mostefa

Materials and Environmental Laboratory, Faculty of Sciences and Technology, University of Medea, Ain D'heb, Medea 26001, Algeria

Received: 10 October 2014
Accepted: 29 December 2014

Abstract

The present work was conducted to optimize operating parameters for electrocoagulation treatment of a pharmaceutical effluent. Chemical oxygen demand (COD) and turbidity removals were monitored for each experiment since they are good indicators of wastewater quality. The effects of three parameters such as pH (4-10), current density (i=20-80 mA/cm²), and time of reaction (t=10-30 min) were evaluated using a response surface methodology (RSM) and in particular a full factorial central composite face-centered (CCF) design. The obtained experimental data were fit to a second-order polynomial equation using multiple regressions and were also analyzed by variance analysis (ANOVA). The contour plots derived from the mathematical models were applied to determine the optimal conditions (pH of 5.31, current density of 46.83 mA/cm², and electrolysis time of 17.99 min). Under these conditions, the experimental COD and turbidity removals were found equal to 75.64 and 96.34%, respectively, which were in agreement with the values predicted by the models. The electrocoagulation mechanism was modeled using Freundlich and Dubinin-Radushkevich isotherms. The obtained results showed that the Freundlich isotherm correctly predicted the experimental data. Operating costs included energy and electrode consumption as performed for the process of treatment. It was noted that the general cost varied from 0.1053-2.8289 US$ for current densities ranging from 20-80 mA/cm² and electrolysis times from 10-30 min. Under optimal conditions, the general cost was found equal to 0.8113 US$/m³.

Keywords: pharmaceutical effluent, electrocoagulation, COD, turbidity, optimization, RSM, isotherm adsorption, operating cost

Introduction

Pharmaceutical industries generate a lot of waste products whose presence in the aquatic environment poses serious problems [1, 2]. It should be noted that tons of different classes of drugs are present in the environment, which are used and extracted through wastewater and sewage treatment plants [3, 4].

The treatment of pharmaceutical effluents and disposal of residual compounds is generally quite complex. Each effluent may have particular characteristics that pose specific problems for treatment [5]. The traditional methods of treatment are essentially biological and physiochemical processes [6-8]. However, these techniques have shown...
limited success for the treatment of pharmaceutical wastewater due to the nature and composition of pharmaceutical effluents. Therefore, other technologies have been explored with the aim to further reduce the concentration of pharmaceutical contaminants. These technologies include membrane separation [9], advanced oxidation technology [10], and electrochemical techniques such as electroflotation and electrocoagulation [11, 12]. Electrocoagulation (EC) has shown the potential to largely overcome the drawbacks of conventional processing techniques.

The EC process is characterized by simple and easy equipment and short operating time without added chemicals. In addition, the benefits of EC compared to conventional chemical coagulation include the reduction of acidification of wastewater and salinity, low doses of coagulant, and the possibility of automating the treatment system [13]. It was reported that EC has been successfully applied for the treatment of wastewater containing different types of contaminants [14, 16].

Various researchers have described the treatment of pharmaceutical wastewaters by electrochemical processes. Jain et al. [17] applied the electrochemical method for the degradation of pharmaceutical azo dye amaranth in wastewater on activated carbon fiber (ACF) electrodes. Dominguez et al. [18] studied the degradation of real pharmaceutical effluent by an electrochemical process with a BDD anode regarding the effect of two operating conditions, such as current density and flow rate at various residence times. Brillas and Sires [19] presented an overview on the electrochemical methods devised for the treatment of pharmaceutical residues from both synthetic solutions and real pharmaceutical wastewaters. Farhadi et al. [20] compared electrocoagulation (EC), photoelectrocoagulation, peroxi-electrocoagulation, and peroxi-photoo electrocoagulation processes used for the removal of chemical oxygen demand (COD) from pharmaceutical wastewater. Boroski et al. [21] applied electrocoagulation using iron electrodes followed by photocatalysis for the treatment of effluents from pharmaceutical and cosmetic factories.

EC is an electrochemical treatment method using sacrificial anodes resulting in the production of active coagulants. In this process, many mechanisms are used to remove pollutants from the aqueous effluents. Anodic oxidation and production of adsorbents (hydrated aluminum hydroxides in the case of aluminum electrodes) occurred simultaneously with cathodic reactions and the evolution of hydrogen gas responsible of absorbent flotation. The metal hydroxides that formed have a large surface and quickly adsorb organic products. Consequently, the formed flocs can be removed by gas flotation or sedimentation.

For a better experimental approach, statistical techniques were preferred for the identification of optimal combination of factors and their interactions. These techniques present the advantages to reduce time and study costs [22]. Response surface methodology (RSM) is a statistical method used for the design of experiments and optimization where the experimental responses are fitted to quadratic functions [23]. RSM was successfully used in the modeling and optimization of wastewater treatment processes [24, 25].

### Table 1. Physicochemical characteristics of the pharmaceutical effluents.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>6.46</td>
</tr>
<tr>
<td>Conductivity (µS/cm)</td>
<td>784</td>
</tr>
<tr>
<td>Turbidity (NTU)</td>
<td>48.60</td>
</tr>
<tr>
<td>COD (mg/L)</td>
<td>525.51</td>
</tr>
</tbody>
</table>

### Table 2. Factors and their levels.

<table>
<thead>
<tr>
<th>Factor</th>
<th>Significance</th>
<th>Experimental Field</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>X₁</td>
<td>pH</td>
<td>4-10</td>
<td></td>
</tr>
<tr>
<td>X₂</td>
<td>Current density</td>
<td>20-80</td>
<td>mA/cm²</td>
</tr>
<tr>
<td>X₃</td>
<td>Time</td>
<td>10-30</td>
<td>min</td>
</tr>
</tbody>
</table>

In this study, electrocoagulation was applied for the treatment of pharmaceutical wastewater using aluminum electrodes. The ions generated from the dissolution of aluminum are used as coagulants for the removal of COD and turbidity. The study was conducted to test the hypothesis that electrocoagulation can be optimized for the three variables usually needed for wastewater treatment (pH, current density, and treatment time). The efficiency of COD and turbidity removals was optimized using RSM and in particular a full factorial central composite face centered (CCF) design. For the description of the adsorption mechanism in terms of COD, Freundlich and Dubinin-Radushkevich isotherms have been applied. Also operating cost (energy and electrode consumptions) during the process of electro-coagulation were calculated.

### Material and Methods

#### Materials

The effluent used in this study was obtained from a pharmaceutical factory (Medea, Algeria) which is a manufacturing unit of oral and injectable pharmaceutical products (antibiotics) that include β-lactam antibiotic derivatives, namely penicillin (ampicillin, oxacillin, and amoxicillin), and tetracycline antibiotics (chlortetracycline and doxycycline).

The effluent was collected from the recovery tank of a sewage treatment plant downstream of a production line of finished product using the grab sampling technique which is usually done by the manual method. All experiments were carried out on the same sample, which has the same physicochemical characteristics. The reagents used in this work were analytical grade and were used without any further purification. The physicochemical characteristics of the effluents from the pharmaceutical unit are shown in

---

**Table 1. Physicochemical characteristics of the pharmaceutical effluents.**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>6.46</td>
</tr>
<tr>
<td>Conductivity (µS/cm)</td>
<td>784</td>
</tr>
<tr>
<td>Turbidity (NTU)</td>
<td>48.60</td>
</tr>
<tr>
<td>COD (mg/L)</td>
<td>525.51</td>
</tr>
</tbody>
</table>

**Table 2. Factors and their levels.**

<table>
<thead>
<tr>
<th>Factor</th>
<th>Significance</th>
<th>Experimental Field</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>X₁</td>
<td>pH</td>
<td>4-10</td>
<td></td>
</tr>
<tr>
<td>X₂</td>
<td>Current density</td>
<td>20-80</td>
<td>mA/cm²</td>
</tr>
<tr>
<td>X₃</td>
<td>Time</td>
<td>10-30</td>
<td>min</td>
</tr>
</tbody>
</table>
Table 1. These characteristics were obtained by the standard test methods, followed by the unit of treatment of the factory which include pH, conductivity, COD, and turbidity.

Experimental Device

The EC apparatus used in this investigation consists of a pair of aluminum electrodes distanced by 1.0 cm. Electrodes were connected to a DC power supplier of 2.5A and 30 V (HPS3025), operating with current density of 20-80 mA/cm². Treatment of samples by electrocoagulation was carried out on a batch-type system using 800 mL of wastewater at different pH values (4-10) and treatment times (10-30 min). The levels of process factors were deduced from the preliminary experiments and literature [26-28]. The pH was adjusted by adding HCl or NaOH. After EC, the treated liquid was analyzed in terms of COD and turbidity. Removal efficiencies (RE) were determined using Eq. (1):

\[ RE(\%) = \frac{(X_i - X_f)}{X_i} \times 100 \] (1)

...where the indices \( i \) and \( f \) correspond respectively to the initial and final measures.

Analytical Methods

The pH of the treated solution was measured using a pH meter (Metrohm). Electric conductivity was measured using a conductometer (type Mettler Toledo EL 30). Turbidity was determined using a turbidity meter (model HF Instruments DRT 100B). COD was determined using a thermoreactor (COD Analysis-ECO 6) complying with the standard NF T90-101.

Operating Cost Calculation

Energy and electrode consumptions are very important economic tools when calculating operating costs for the electrocoagulation process. Other costs such as labor, maintenance, and other provisions are assumed to be fixed and are not included in the calculations [29, 30]. Operating cost (OC) can be calculated by the following relation (Eq. (2)):

\[ OC = X \cdot E_c + Y \cdot E_{el} \] (2)

...where \( E_c \) is energy consumption and \( E_{el} \) is electrode consumption for pollution removal. \( X \) and \( Y \) are the prices of electricity and electrode materials, respectively. The prices obtained from the Algerian market in September 2013 are as follows: \( X = 0.0423 \) US$/kWh, and \( Y = 0.3 \) US$/kg for aluminum.

Energy consumption (\( E_c \)) was calculated from the expression:

\[ E_c = \frac{U \cdot I \cdot t \cdot V}{V} \] (3)

...where \( U \) is cell voltage (V), \( I \) is current (A), \( t \) is time of electrolysis (s), and \( V \) is the volume (m³) of treated wastewater.
Electrode consumption \((E_{el})\) can be calculated by the relation (Eq. (4)) [29]:

\[
E_{el} = \frac{I \cdot t \cdot M}{z \cdot F \cdot V}
\]

...where \(I\) is the current (A), \(t\) is the time of electrolysis (s), \(M\) is the molecular mass of aluminum (26.98 g·mol\(^{-1}\)), \(z\) is the number of electrons transferred (\(z=3\)), \(F\) is Faraday’s constant (96500 C·mol\(^{-1}\)), and \(V\) is the volume (m\(^3\)) of the treated wastewater.

Experimental Design

A full factorial central composite face-centered (CCF) design was used in order to investigate the influence of the experimental factors and their interactions on COD and turbidity removals and to make predictions for different input values. The CCF design was chosen because it provides relatively high-quality predictions over the entire design space and does not require using points outside the original factor range [31]. This design was used for the optimization of various treatment processes [32, 33].

The medium components (independent variables) selected for optimization were pH \((X_1)\), current density \((X_2)\), and time treatment \((X_3)\). The responses are \(Y_1\) (% of COD removal) and \(Y_2\) (% of turbidity removal). Regression analysis was performed on the data obtained from the experiments. Coding of the variables was done according to the following equation:

\[
x_i = \frac{X_i - X_{cp}}{\Delta X_i}, \quad i = 1, 2, 3\ldots, k
\]

...where \(x_i\) is a dimensionless value of an independent variable, \(X_i\) is a real value of an independent variable, \(X_{cp}\) is a real value of an independent variable at the center point, and \(\Delta X_i\) is a step change of a real value of the variable \(i\) corresponding to a variation of a unit for the dimensionless value of the variable \(i\).

The original levels for the process factors are shown in Table 2. The experiments were carried out in duplicate, which was necessary to estimate the variability of measurements.

The relationship of the independent variables and the responses were calculated by the second-order polynomial equation (Eq.6):

\[
Y = \beta_0 + \sum_{i=1}^{4} \beta_i x_i + \sum_{i=1}^{4} \beta_i^2 x_i^2 + \sum_{i=j}^{n} \sum_{j=1}^{n} \beta_{ij} x_i x_j
\]

...where \(Y\) denotes the predicted response; \(x_i\) refers to the coded levels of the input variables; \(\beta_0, \beta_i, \beta_{ii}\) and \(\beta_{ij}\) are the regression coefficients (off set term, main, and quadratic and interaction effects); and \(n\) is the total number of designed variables. The coefficient values of Eq. (6) were calculated and tested for their significance [34, 35].

Model fitting and graphical simulations were obtained using Modde-6 software (Umetrics).
Adsorption Isotherms

In the case of an aqueous suspension, the solid/liquid equilibrium is studied through the determination of the adsorption isotherm. It shows the variation of the adsorbed quantity \( q_e \) on a solid according to the balance of the equilibrium concentration of the adsorbable compound \( C_e \), at a specific temperature. The curves \( q_e=f(C_e) \) represent the adsorption isotherms, which are determined experimentally. The experimental data can then be correlated with mathematical models representing the best experimental adsorption isotherms in a wide range of concentrations and temperatures. A large number of adsorption isotherm models have been developed by different researchers. Among these isotherms, Langmuir and Freundlich are commonly used for the determination of the maximum adsorption capacity of the material, and the adsorption constant \( K_a \) characterizes the adsorbent-adsorbate interactions [36, 37]. From these isotherms, two parameters can be deduced, the equilibrium constant adsorbate-adsorbent and the adsorption energy. Even more recent models of Kiselev and Dubinin-Radushkevich (D-R) are used for the determination of the constant of the formation of the complex between adsorbed molecules and solid surface [37].

In this work two models were employed: Freundlich and Dubinin-Radushkevich isotherms. The first one is empirical and usually gives a very good representation of the experimental results, and the second is generally applied in order to find out the adsorption mechanisms.

The Freundlich equation is based on adsorption on heterogeneous surfaces. It is used in the case of a possible formation of more than one monolayer of adsorption on the surface, and the sites are heterogeneous with different energies of fixation. The isotherm is expressed by the equation:

\[
q_e = k_f \cdot c_e^{1/n}
\]  

This equation can be linearized as follows:

\[
\ln q_e = \ln k_f + \left(\frac{1}{n}\right) \cdot \ln c_e
\]  

...where \( k_f \) (mg/L) is the Freundlich adsorption constant and \( n \) a constant depending on the nature of the adsorbate and temperature (0.3<\(n<0.5 \)) for a good model verification).

The Dubinin-Radushkevich isotherm is generally applied to express the adsorption mechanism with a Gaussian energy distribution onto a heterogeneous surface [38]. The equation is expressed as follows:

\[
q_e = q_m \exp(-\beta \epsilon^2)
\]  

Eq. 9 can be linearized as:

\[
\ln q_e = \ln q_m - \beta \epsilon^2
\]  

...where \( q_m \) represents the maximum theoretical capacity of adsorbate adsorbed on the solid surface and \( \epsilon \) corresponds to the Polanyi potential. This potential is given by Eq. 11:

\[
\epsilon = RT \ln(1 - (1/Ce))
\]  

...where \( R \), \( T \), and \( Ce \) represent the gas constant, absolute temperature, and adsorbate equilibrium concentration, respectively.

The constant \( \beta \) represents the adsorption of molecules on the adsorbent following its transfer from the solution. \( \beta \) and energy \( E \) are related by the following equation [39]:

\[
E = 1/(2\beta)^{1/2}
\]  

Thus, by plotting \( \ln(q_e) \) versus \( \epsilon^2 \), it is possible to obtain the value of \( q_m \) and \( \beta \). The values of \( E \) indicate if the adsorption follows an ion exchange mechanism or a physical adsorption mechanism. If \( E \) is between 8 and 16 kJ/mol, the process follows ion exchange adsorption, whereas for values of \( E<8 \) kJ/mol, the adsorption process is physical, and if \( E>16 \) kJ/mol the process is dominated by diffusion intra-particles [40].

Results and Discussion

Analysis of Design of Experiments

The arrangements of CCF design include 16 sets of electrocoagulation experiments, including three repetitions for the calculation of the pure error (Table 3).

By using multiple regression analysis, the responses were correlated with the three design factors using the second-order polynomial (Eq. (3)). The quadratic regression models for COD (\( Y_1 \)) and turbidity (\( Y_2 \)) are given by Eq. (13) and Eq. (14), respectively:

\[
Y_1 = 54.9854 – 20.6256 X_1 – 7.11003 X_2 + 3.24999 X_3 + 0.184353 X_3^2 – 0.0733418 X_1 X_2 – 11.14996 X_2 X_3 + 0.745792 X_1 X_3 + 1.156739 X_2^2
\]  

\[
Y_2 = 98.8728 + 2.37251 X_1 + 0.609592 X_2 + 0.0424751 X_1^2 + 1.35475 X_1 X_2 + 0.368543 X_2^2 + 0.184353 X_1^2 – 0.0733418 X_2 X_3 – 0.685851 X_2 X_3^2 – 0.731546 X_3 X_2
\]  

The overall analysis of the models consists in determining the values of the coefficients of determination (\( R^2 \)). \( R^2 \) was equal to 0.970 for turbidity (Table 4), indicating that 97% of the variability in the response could be explained by the model. Only 3% of the total variation cannot be explained by the model. The adjusted determination coefficient (\( R_{adj}^2=0.924 \)) was also satisfactory, confirming the significance of the model. For COD removal, \( R^2 \) was 0.877, suggesting an acceptable correlation between the predicted values and the experimental results; this indicates that only 12.3% of the total variation could not be explained by the empirical model and expresses well enough how quadratic fits to navigate the design space. These values confirm that the equations of the models are reliable. This also indicates that the model terms are significant. The models are also reproducible (values of reproducibility close to 1).
Plots giving the predicted values versus observed values (Figs. 1 and 2) show that the second-order polynomial models correlate well the experimental results.

In order to test the validity of the models, analysis of variance (ANOVA) was employed to examine the meaning and the adequacy of the models. The results of ANOVA for the quadratic models summarize the analysis of each response and show the significant model terms. Table 4 summarizes ANOVA results for COD and turbidity removals (Y1 and Y2).

The significance of each coefficient was evaluated by p-value and standard error (Table 5). A small p-value (less than 0.05) indicates that model terms are significant. The analysis of variance reveals that a second-order model adequately fits the experimental data for all responses. For COD removal, it was noted that linear effects of pH (X1), and the interaction term between pH and reaction time (X1X3) are significant models. Linear effects of (X2), (X3), the quadratic contribution of X12, X22, X32, and the interaction term between X1X2 and X2X3 does not affect COD removal. However, for turbidity removal it was noticed that the linear effects of X1 and X2, and the interaction term between (X1X3) and (X2X3) and the quadratic contribution X12 are significant models. Other coefficients such as (X3), X22, X32, and X1X2 are found to be insignificant.

**Effect of Factors on COD and Turbidity Removals**

The own effect of the main factors and their interactions on the responses can be deduced by simulation. Fig. 3 shows the effects of treatment factors and their interactions on COD and turbidity removals from a real pharmaceutical effluent. These effects represent the coefficients in the surface response models (Eqs. (13) and (14)). A coefficient with a plus sign (+) means that the factor has a synergistic effect. By varying the factor the response increases and a minus sign (-) shows an antagonistic effect factor; this suggests that by varying the factor the response decreases. It was noticed that pH (X1), current density (X2), and reaction time (X3) have negative effects on COD removal, but they have a positive effect on turbidity removal. Decreasing
in initial pH, current density, and reaction time result in increasing COD removal, but there was little effect on turbidity removal percentage. It was observed that the interaction terms $X_1X_3$ and $X_2X_3$ have a positive effect on COD removal, but a negative effect on turbidity removal. Unlike the interaction term, $X_1X_2$ have a negative effect on both COD and turbidity removals. The second-order terms $X_i^2$ have a negative effect on COD and a positive effect on turbidity removal. Finally, the second-order terms $X_2^2$ and $X_3^2$ have a negative effect on COD but a positive effect on turbidity removal.

In order to investigate the interactions between different independent variables and their corresponding effects on the responses, contour plots were drawn (Figs. 4-6). The contour plot is a graphical representation of a three-dimensional response surface as a function of two independent variables, maintaining all other variables at a fixed level. These plots can be helpful in understanding both the main and interaction effects of the independent variables on the responses. Fig. 4 shows the effects of pH and current density on COD and turbidity removals, reaction time was maintained constant at central value (20 min). The effect of pH can be explained considering aluminum and antibiotics (tetracycline and b-lactam derivatives) equilibrium related to the pH values. It was noted that high COD removal was found at pH≤5, and a current density between 20 and 65 mA/cm². The increase in COD removal at this level of pH can be explained by the transformation of Al\(^{3+}\) into soluble monomeric species such as Al(OH)\(_2^+\) and Al(OH)\(_3^-\) in acid medium, and Al(OH)\(_4^-\) in alkaline medium.

These species are converted into insoluble Al(OH)\(_3\) flocs by complex precipitation kinetics. Freshly formed amorphous Al(OH)\(_3\) can absorb ions and even soluble organic compounds and/or trap colloidal particles, which then coagulate to produce particles that precipitate, usually near neutral pH. It is important to note that under acidic conditions (pH<3), penicillins undergo isomerization linked to the breakdown of the beta-lactam ring and the formation of the imidazoline ring, turning into penillic acids and TC exists as TCH\(_3^+\).

At pH between 3.3 and 7, TC exists as TCH\(_2^-\), due to the loss of proton from the phenolic diketone moiety. At pH≥10, where TC presents as TC\(^-\) and penicillin is in the anionic form, Al (OH)\(_4^-\) is dominant and consequently the coagulation rapidly decreases [19, 40-44]. However, the effects of pH and current density on turbidity removal are not important because there was not a remarkable change in the elimination rate of turbidity (≈ 93-100%). This result can be explained by the low variation of turbidity of pharmaceutical effluents.

The effects of pH and time reaction are shown in Fig. 5. Current density was kept constant at central value (i=50 mA/cm²).
mA/cm²). From the contour plot it was noticed that COD removal took maximum values if initial pH was maintained fewer than 5 and time treatment between 10 and 22 min. For these conditions, turbidity varied slightly and we didn’t notice important effects.

In order to investigate the effect of current density and time reaction on COD and turbidity removals, experiments were conducted at pH=7 under different operating times and current densities. The results are presented in Fig. 6, where the contours clearly show an optimum zone of COD removal at a current density between 32.3 and 42.9 mA/cm² and time treatment between 17.4 and 21.8 min. COD removal decreases with increasing current density beyond 50 mA/cm². It is well known that EC is strongly affected by the current density [45]. This effect can be explained by the fact that an increase in anodic dissolution of aluminum occurs with high current density, which results in the formation of high amounts of precipitate for the removal of pollutants. Furthermore, the rate of production of hydrogen bubbles increases and their sizes decrease as the current density increases. All these effects are beneficial for effective removal of pollutants. Operating at high current densities may cause other side reactions in the vicinity of the anode, such as the direct oxidation of one of the constituents of the contaminant or the formation of oxygen, which limits the effectiveness of electrocoagulation. Conversely, a high current density causes passivity of the cathode by reduction, leading to a high consumption of energy by the Joule effect. It would be interesting to work on slightly high current densities. From a consumer perspective, especially regarding energy and electrode consumptions, the best conditions correspond to a low current density and an important electrolysis time. To overcome the unnecessary generation of Al(OH)₃ in wastewater, it is ultimately important to avoid working at too high current densities and set to i values less than 50 mA/cm². The efficiency of contaminant reduction depends on Al (III) production by the anode so that high electrolysis duration would cause higher production of these aluminum hydroxide, which are in turn responsible for the coagulation process. As shown in Table 3, COD and turbidity removals also increased as a function of time, and after 22 min of electrolysis no efficacy changes are observed as the EC duration is increased.

### Optimization

The main objective of optimization is to determine the optimum parameters for COD and turbidity removal during the process of electrocoagulation. To control the optimization criteria the weight function has a key role, as well as reasonable limits and targets for the responses. The optimizer of the Modde software uses a Nelder Mead Simplex method with the fitted response functions to optimize an overall desirability function combining the individual desirability of each response. The shape of the desirability function is controlled by the weight and the settings of criteria (Min, Target, Max) for each response.

For each optimum found, the software provides the optimal values of input factors, the response values predicted by the model, the number of iterations until the optimum, and the logarithm of the overall distance to the target named as Log(D).

The “overall distance to target,” D, is computed by the following equation [46]:

$$D = \log_{10} \left[ \sum (w_i (y_i - T) / (T - L))^2 / M \right]$$  \hspace{1cm} (15)

...where $w_i$ is the assigned weight representing the importance of the response, $y_i$ is the response to be maximized or minimized, $T$ is the user-desired target, $L$ is the user-defined worst acceptable response value, and $M$ is the number of responses.
A maximum overall desirability function results in a minimum Log(D). For optimization, D is not used but it is displayed as Log(D) in the run list. When Log(D)=0, all responses are between the target and the specified acceptable limit. Log(D) becomes negative when the values of all responses are still closer to the target. The value of D is equal to -10 when all responses have reached T.

Fig. 7 displays, for each simplex, the value of Log(D) vs. iteration number. The target and acceptable limit(s) are drawn for every response as lines (Fig. 8). It was noticed that not all responses are between the target and acceptable limit, but some are between the min and the target.

Table 6 shows the run list, which includes the factors, responses, iterations, and Log(D). After running the opti-
mizer for the best proposal, lowest Log(D) is selected. In the run list above, row 1 has the lowest Log(D) (iteration 107), meaning that row 1 is preferable. The optimal parameters for COD and turbidity are pH=5.31, current density=46.83 mA/cm², and reaction time=17.99 min.

These obtained results were compared with those deduced from the contour plots. At optimal conditions, COD and turbidity removals are 70.8% and 96.7%, respectively. These results are close to those estimated by the optimizer software.

In order to confirm the validity of the statistical experimental strategies, experiments under optimal conditions were realized. The average measured COD and turbidity removals are respectively equal to 75.64 and 96.34%. This experimental validation proved that the developed models could be considered to be accurate and reliable.

**Isotherm Modeling**

To investigate the equilibrium isotherms of adsorption in term of COD, four experiments were taken from the experimental design matrix. Freundlich and Dubinin-Raduskovich parameters for COD removal are summarized in Table 7. Freundlich adsorption capacity was found to be 0.0059 L/mg. From the linear plot of the Dubinin-Raduskovich model, qm was determined and its value is about 306.12 mg/g. The mean free energy (E) is equal to 0.0062 kJ/mol. This value indicates that the process of adsorption is a physisorption process and that the van der Waals forces are predominant. These results are in agreement with the mechanism of electrocoagulation. It is generally assumed that in the electrocoagulation process, the coagulation is provoked essentially by the reduction of the net surface area charge...
until the colloidal particles, previously stabilized by electro-
static repulsion, can get closer to the van der Waals forces to
hold them together and allow aggregation. Figs. 9 and 10
show that the COD experimental measurements give a good
fit for the Freundlich isotherm model with a good linear
regression coefficient ($R^2 = 0.972$), and an acceptable fit for
the Dubinin-Raduskovich isotherm ($R^2 = 0.914$). However,
the Freundlich isotherm seems to be better than the Dubinin-
Raduskovich isotherm. It can be concluded that the nature of
the aluminum surface is more heterogeneous.

The experimental results plotted against the Dubinin-
Raduskovich and Freundlich adsorption isotherms are
shown in Fig. 11. Comparison of the results reveals that the
Freundlich adsorption isotherm was the best model for
COD adsorption. Hence the values predicted by the
Freundlich model are close to the experimental data for the
values of $C_e$ less than 300 mg/L, whereas at higher values
of $C_e$ this model shows little difference compared to the
experimental data.

**Operating Cost**

Variations of the operating costs for the treatment of
pharmaceutical wastewater are presented in Fig. 12. When
the current density enhanced from 20 to 80 mA/cm² and
reaction time from 10 to 30 min, electrode consumption
was enhanced from 0.02471536 to 0.49721484 kg/m³ and
energy consumption enhanced from 0.7366 to 37.2968
kWh/m³. It was noticed that the maximum operating cost
was found to be equal to 2.8289 US$/m³, which corre-
sponds to a current density of 80 mA/cm² and electrolysis
time of 30 min. This is caused by the increase in the rate of
dissolution of the metal and the high level of energy con-
sumption. The minimum operating cost was observed at a
current density of 20 mA/cm² and electrolysis time of 10
min, which was equal to 0.1053 US$/m³. This corresponds
to low metal dissolution and low consumption energy.
According to these results, there is a direct relationship
between current density, electrolysis time, and operating
cost. This cost increases with increasing current density,
electrolysis time, and vice versa. The energy consumption
is affected by the charge loading ($Q=I·t$) and electrolysis
potential. A higher charge loading will increase energy and
electrode consumption. Charge loading is very important

![Fig. 9. Freundlich isotherm adsorption.](image)

![Fig. 10. Dubinin-Radushkevich isotherm adsorption.](image)

![Fig. 11. Experimental, Freundlich, and Dubinin-Radushkevich
model values of $q_e$ versus $C_e$.](image)

![Fig. 12. Evolution of operating cost in the experiments of electrocoagulation treatment.](image)
Conclusions

In the present work the electrocoagulation process was used for the treatment of a pharmaceutical wastewater using aluminum electrodes. A full factorial central composite face-centered (CCF) design was successfully employed for the experimental design and analysis of results.

This study clearly showed that RSM was one of the suitable methods to optimize the operating conditions and maximize COD and turbidity removal. The obtained correlation coefficient R² was found equal to 0.97 for COD and 0.877 for turbidity removal, indicating that the actual data fit quite well with the predicted data by applying the quadratic models. The effects of pH, current density, and electrolysis time on optimal operational conditions were evaluated. The optimum of turbidity and COD removal efficiencies were found at initial pH of 5.31, current density of 46.83 mA/cm² and reaction time of 17.99 min. The corresponding removal efficiencies in optimum conditions were found equal to 70.8% and 96.7% for COD and turbidity removal, respectively.

Experimental data were modeled using adsorption isotherms. Comparison of results revealed that the Freundlich isotherm (R² =0.972) was better suited than the Dubinin-Raduskovich model (R² =0.914). The mode of adsorption is a physisorption with heterogeneous aluminum surface. Under optimal conditions, the operating cost was found equal to 0.8113 US$/m³, which can be considered an economical process.

References


