

Table 1. Development Level Grade Standards

Index	Grade
$0 \leq S < 0.25$	Raised
$0.25 \leq S < 0.50$	Ordinary
$0.50 \leq S < 0.75$	Good
$0.75 \leq S < 1.00$	Excellent

Coupling Coordination Model

In order to further study the coordination relationship between the low-carbon economy and the energy structure, so as to more intuitively reflect the development of cities in Anhui Province, this paper studies the coupling relationship between the two with the help of the coupling coordination model [34-36]:

$$C = 2 \left[\frac{(S_L S_E)}{(S_L + S_E)^2} \right]^{\frac{1}{2}} \quad (6)$$

$$T = \alpha \times S_L + \beta \times S_E \quad (7)$$

$$\alpha = 1 - \beta \quad (8)$$

$$D = \sqrt{CT} \quad (9)$$

Among them, S_L and S_E represent the development level of low-carbon economy and energy structure, C represents coordination relationship degree, and C represents the relationship between low-carbon economy and energy structure. T represents the comprehensive development level index, α and β represent the comprehensive development level index coefficient. In view of the mutual promotion and complementarity between the low-carbon economy and the energy structure, the values of 0.5 for α and β respectively indicate that they are equally important. D indicates the coupling degree between low-carbon economy and energy structure.

With reference to the relevant evaluation criteria for the coupling development of low-carbon economy and energy structure [35,36], and in combination with the actual situation of energy economic development in Anhui Province, the coupling degree is divided into 3 coupling regions and 10 coupling grades, as shown in Table 2.

Table 2. Coupling Grade Standards

Coupling region	Coupling grade	Coupling degree-D	Coupling region	Coupling grade	Coupling degree-D	Coupling region	Coupling grade	Coupling degree-D
Disharmonic	Extreme imbalance	0-0.1	Adaptive	Near imbalance	0.4-0.5	Benign	Primary coordination	0.6-0.7
	Severe imbalance	0.1-0.2					Moderate coordination	0.7-0.8
	Moderate imbalance	0.2-0.3		Barely coordination	0.5-0.6		Good coordination	0.8-0.9
	Mild imbalance	0.3-0.4					High quality coordination	0.9-1.0

Traditional GM (1,1)

The grey model [20, 37] transforms the original data into a regular sequence through the degree of dissimilarity between factors, and establishes a differential equation model to predict development trends. The most commonly used model is GM (1,1):

(1) Accumulated generation:

Accumulate the sequence $x^{(0)} = (x^{(0)}(1), x^{(0)}(2), \dots, x^{(0)}(n))$ to obtain the

1-AGO sequence $x^{(1)} = (x^{(1)}(1), x^{(1)}(2), \dots, x^{(1)}(n))$,

$$x^{(1)}(t) = \sum_{k=1}^t x^{(0)}(k), t = 1, 2, \dots, n.$$

(2) First fit parameters:

Solve the differential equation of GM (1,1) model:

$$\frac{dx^{(1)}(t)}{dt} + ax^{(1)}(t) = b \quad (10)$$

By solving equation (10), the time response function can be obtained:

$$\hat{x}^{(1)}(t+1) = (x^{(0)}(1) - \frac{b}{a})e^{-at} + \frac{b}{a}, t = 1, 2, \dots, n \quad (11)$$

(3) Determine the predicted value, and the prediction function is:

$$\hat{x}^{(0)}(t+1) = \hat{x}^{(1)}(t+1) - \hat{x}^{(1)}(t) = (1-e^{-a})(x^{(0)}(1) - \frac{b}{a})e^{-at}, t = 1, 2, \dots, n \quad (12)$$

(4) Accuracy inspection

To verify the reliability of the model, it is necessary to verify the accuracy of the model. In this study, relative residual and class ratio dispersion were used, and the mean relative residual was calculated using formula (13), while the mean class ratio dispersion was calculated using formula (14).

$$\bar{\varepsilon}_\gamma = \frac{1}{n-1} \sum_{k=2}^n \left| \frac{x^{(0)}(k) - \hat{x}^{(0)}(k)}{x^{(0)}(k)} \right| \times 100\%, k = 2, 3, \dots, n \quad (13)$$

$$\bar{\eta} = \sum_{k=2}^n \frac{\left| 1 - \frac{1-0.5\hat{\alpha}}{1+0.5\hat{\alpha}} \frac{1}{\sigma(k)} \right|}{n-1}, k = 2, 3, \dots, n \quad (14)$$

If $\bar{\varepsilon}_y$ or $\bar{\eta}$ is less than 20%, the fitting effect reaches the general required level. If $\bar{\varepsilon}_y$ or $\bar{\eta}$ is less than 10%, the fitting effect reaches a very good level.

GM (1,1) for Multi Algorithm Optimization

With the development of grey systems, the information significance of old data continues to decrease. While constantly supplementing new information, timely removal of old information can better reflect existing feature patterns. It is clearly necessary to remove old data that cannot reflect the current characteristics of the system. Therefore, this article selects the new information GM (1,1) and metabolic GM (1,1) for comparative analysis with traditional GM (1,1) [38-40].

(1) New Information GM (1,1)

The model established using $X^{(0)} = (x^{(0)}(1), x^{(0)}(2), \dots, x^{(0)}(n), x^{(0)}(n+1))$ is called New Information GM (1,1). Set $x^{(0)}(n+1)$ as the latest information and place $x^{(0)}(n+1)$ in $X^{(0)}$.

(2) Metabolic GM (1,1)

The model established using $X^{(0)} = (x^{(0)}(2), \dots, x^{(0)}(n), x^{(0)}(n+1))$ is called Metabolism GM (1,1). Insert the latest information $x^{(0)}(n+1)$ and remove the oldest information $x^{(0)}(1)$.

Resistance Model

In order to ensure the rational allocation and optimization of energy economy, formulate and adjust comprehensive governance policies, and use the resistance model [26] to diagnose the key resistance factors in the

coupling relationship between low-carbon economy and energy structure in Anhui Province.

The resistance value O represents the degree of resistance of the factor; Skewness $s_{ij} = 1 - x_{ij}$ represents the difference between the factor and the optimal value; Contribution degree w_j (weight) represents the contribution size of the factor:

$$O = \frac{s_{ij} w_j}{\sum_{j=1}^n (s_{ij} w_j)} \quad (15)$$

Result

Construction of Evaluation Indicator System

Drawing on the scientific research achievements of scholars, combining the principles of accessibility, representativeness, and operability of evaluation indicators, 12 evaluation indicators are selected to build a comprehensive evaluation indicator system from the two dimensions of energy structure and low-carbon economy, and based on the SDI conceptual framework model of "State-Danger-Immunity". See Table 3 for details.

Analysis of Development Level

The development index and development grade evaluation results of low-carbon economy and energy structure in Anhui Province from 2014 to 2021 are shown in Table 4.

Table 3. Comprehensive Evaluation Indicator System

Target layer	State layer	Indicator layer	Indicator code	Indicator attribute	Indicator unit
Energy structure	S	Total energy production	I ₁	+	Ten thousand tons of standard coal
	D	Total energy consumption	I ₂	-	Ten thousand tons of standard coal
	I	Energy processing conversion efficiency	I ₃	+	%
	S	Total per capita water resources	I ₄	+	Cubic meter per person
	D	Sudden environmental incidents caused by water pollution	I ₅	-	Piece
	I	Budget expenditure for agriculture, forestry, and water	I ₆	+	100 million yuan
	S	GDP of tertiary sector of the economy	I ₇	+	100 million yuan
Low-carbon economy	D	Traffic accident situation	I ₈	-	Piece
	I	Public safety budget expenditure	I ₉	+	Hundred million yuan
	S	Gross industrial product	I ₁₀	+	Hundred million yuan
	D	Industrial sewage discharge per ten thousand yuan of GDP	I ₁₁	-	Ton
	I	Investment in industrial wastewater treatment	I ₁₂	+	Ten thousand yuan

of the coupling coordination model, and the GM (1,1) optimized by various algorithms is used to predict Anhui Province. From 2014 to 2021, the coupling development of low-carbon economy and energy structure in Anhui Province showed a steady upward trend. There is a trend towards primary coordination at the coupling grade, with the coupling area developing into benign. From 2022 to 2026, the coupling development of low-carbon economy and energy structure in Anhui Province will be stable and good.

It can be seen that the coupling development of low-carbon economy and energy structure has been rising steadily, and it is hoped that the coupling grade will rise to moderate coordination, and that the coupling region is still benign. The government should promote green and low-carbon energy development, vigorously develop non fossil fuels, and improve the level of clean and efficient utilization of fossil fuels [43]. The premise is to focus on energy resource endowments, continuously enhance energy supply guarantee capabilities, accelerate the construction of a new energy system, and promote a significant increase in the proportion of clean energy consumption, in order to ensure significant results in the green and low-carbon transformation of the energy structure.

Conclusions

Based on the SDI conceptual framework and from the two dimensions of energy structure and low-carbon economy, this paper selects 12 indicators to build an evaluation indicator system. Evaluate development level using the development index, measure coupling level using the coupling degree, predict future coupling level using the grey model optimized by multiple algorithms, and finally use resistance value for the resistance diagnosis.

- (1) The overall development level of the energy structure shows a downward trend, first increasing and then decreasing, reaching its highest level in 2015. The development level of the low-carbon economy is on the rise as a whole, and it only declined in 2017. It has been growing steadily before and after, and will reach its highest level in 2021. The development grade of the energy structure dropped from the ordinary level to the raised level, and the development grade of the low-carbon economy rose from the raised level to the ordinary level after fluctuating growth.
- (2) From 2014 to 2026, the coupling development of low-carbon economy and energy structure in Anhui Province shows a steady upward trend. There is a trend towards primary coordination at the coupling grade, with the coupling area developing into benign. From 2014 to 2015, the coupling degree was between 0.3 and 0.4, with a mild imbalance in the coupling grade and disharmony in the coupling region. In 2016, it was between 0.5 and 0.6, with a coupling grade of barely coordination and an adaptive coupling area. From 2017 to 2020, the coupling degree was between 0.4 and 0.5, and the coupling grade was near imbalance, with the coupling area being adaptation. From 2021 to 2025, it will be between 0.5 and 0.6, with a coupling grade of

barely coordination and an adaptive coupling area. In 2026, it will reach its highest level, with the coupling grade rising to primary coordination and the coupling area reaching benign.

- (3) From 2014 to 2021, the overall resistance in the energy structure dimension showed a steady growth trend, and the overall resistance in the low-carbon economy dimension showed a steady downward trend. The key resistance factors restricting coupling development in 2014 are mainly concentrated in the low-carbon economy dimension. The key resistance factors restricting coupling development in 2017 are still mainly concentrated in the low-carbon economy dimension. The key resistance factors restricting coupling development in 2021 are mainly concentrated in the energy structure dimension, but the first resistance factor is in the low-carbon economy dimension.

But there are still some limitations to this article. Firstly, in terms of research objects, this article only selected Anhui Province as an example to analyze its temporal variation characteristics, but did not take into account the spatiotemporal differences between cities or counties in Anhui Province. Secondly, in terms of weighting evaluation indicators, this study only used the entropy weighting method and only considered objective factors, without combining subjective and objective weighting. Finally, in the selection of prediction methods, the sum of squares of errors of the three prediction methods used in this article are all very small, with values around 0.007. The new information model used for prediction has a mean relative residual of about 0.08 and a mean class ratio dispersion of about 0.12. The fitting effect is good, but they are all based on algorithm improvements based on GM (1,1) and have not been compared and analyzed with other prediction methods.

So in the following research, spatial heterogeneity analysis can be selected from various cities or counties in Anhui Province. At the same time, the combination weighting method can be used to effectively combine objective weighting and subjective weighting. In order to make the prediction results more accurate, the prediction methods of the BP neural network model, LSTM model, etc. can be compared and analyzed.

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Conflicts of Interest

The authors declare no conflict of interest.

